

## Math 100 - Week 3 Recitation (Fall 2013)

So far we've developed two major techniques for taking antiderivatives:  $u$ -substitution and integration by parts. For the integrals in Problems 1 through 10, your goal is to determine whether solving the integral would require:

- (A) Substitution  
(B) Integration by parts  
(C) Both of these methods  
(D) Neither of these methods

Note that figuring out which method to use might not require you to completely solve the integral. You should start by discussing with your group what strategy you would use for each integral, and then "check your work" by solving as many integrals as you have time for. You should probably prioritize the integrals you are the least sure about!

1.

$$\int x^5 e^x dx$$

6.

$$\int x^5 \sqrt{x^6 + 1} dx$$

2.

$$\int x^5 \sin(x^6) dx$$

7.

$$\int (x^5 + x^2) \ln x dx$$

3.

$$\int x^3 e^{(x^4)} dx$$

8.

$$\int \frac{1}{\sqrt{1-x^2}} dx$$

4.

$$\int x^9 \sin(x^5) dx$$

9.

$$\int \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$$

5.

$$\int (x^5 + 1)(x^6 + 1) dx$$

10.

$$\int e^{\sqrt{x}} dx$$

11. (Challenge problem!) Suppose that after  $t$  seconds, starting at time  $t = 1$ , an object is  $\sin(\ln t)$  meters above the ground. Note that the object is on the ground at time  $t = 1$ .
- (a) At what time will the object first hit the ground again?
- (b) Find the average height of the object during the time between when the object leaves the ground ( $t = 1$ ) and when it first hits the ground again.